

Generation of planetary core zonal flows by orbital forcings or fingering convection



D. Cébron^{1*}, R. Monville¹, J. Vidal¹, A. Sauret² & N. Schaeffer¹

¹ISTerre, Grenoble Alpes University, Grenoble ; ²Dpt. of Mech. Eng., Univ. of California, Santa Barbara, USA
 *David.cebron@univ-grenoble-alpes.fr ; work funded by the ERC THEIA (grant agreement no. 847433)

Zonal flows (ZF) generation is a **long-standing issue** in rotating fluids, possibly key for the dynamics of **planetary fluid layers** (e.g. planetary liquid cores). These flows can indeed modify angular **momentum exchanges** between liquid and solid layers¹. Moreover, they can be **unstable**^{2,3}, which could sustain **space-filling turbulence** and **mixing**.

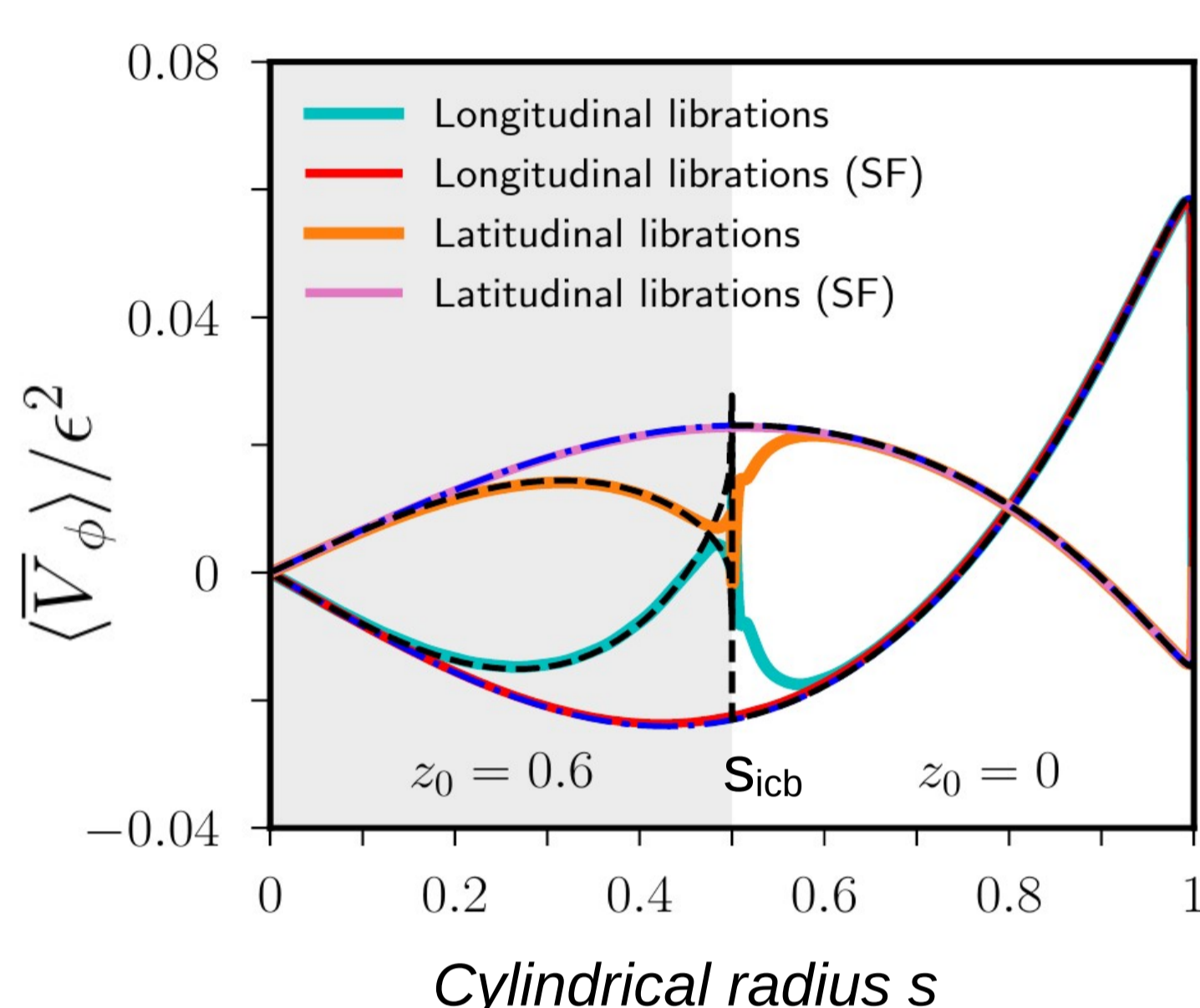
ZF of planetary liquid cores are usually studied as emerging from convection in rapidly **rotating fluid-filled spheres**. Here, we consider **two alternative origins** for such flows:
(1) Orbital forcings (e.g. tides, precession), notably through **nonlinear effects within the Ekman layer**⁴. These flows are of interest because they survive in the relevant planetary regime of both vanishing forcings and viscous effects. Their presence, and the competition with bulk driven zonal flows, are considered for various planets and moons.
(2) Rotating double-diffusive convection (RDDC) in stably stratified planetary cores⁵. Equatorially symmetric & antisymmetric large-scale ZF are found. Considering the early Earth core, we find that double diffusion can reduce the critical Rayleigh number by **four decades**, and we suggest that it was prone to **turbulent RDDC**, with large-scale ZF.

Zonal flows due to orbital forcings⁴

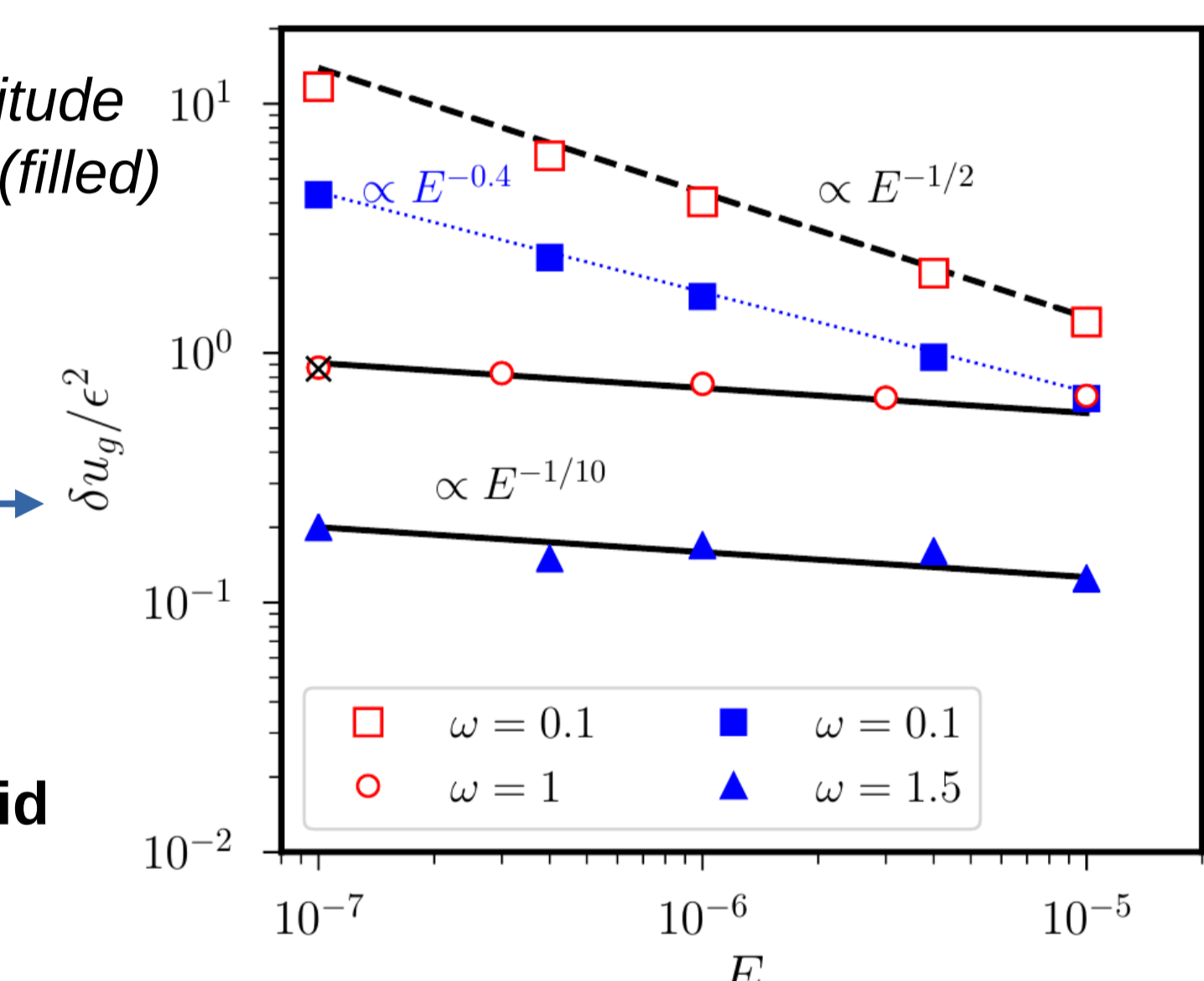
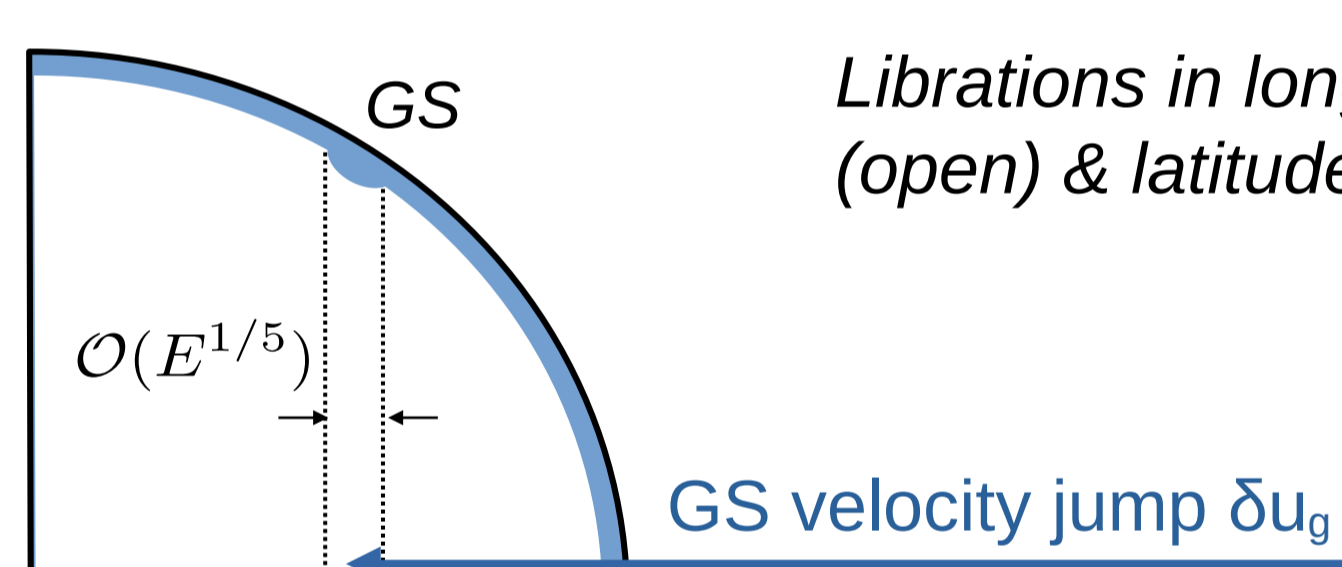
Method : theory & simulations

- **Boundary-layer theory**
- **Weakly nonlinear effects**
- **Spatial & temporal perturbations**
- **Extended to spheroids**
- **Validation: XSHELLS & NEK5000**

- => **Good agreement, even with**
- **spheroidal shell geometries**
- **different inner & outer flattenings**
- **different inner & outer forcings**



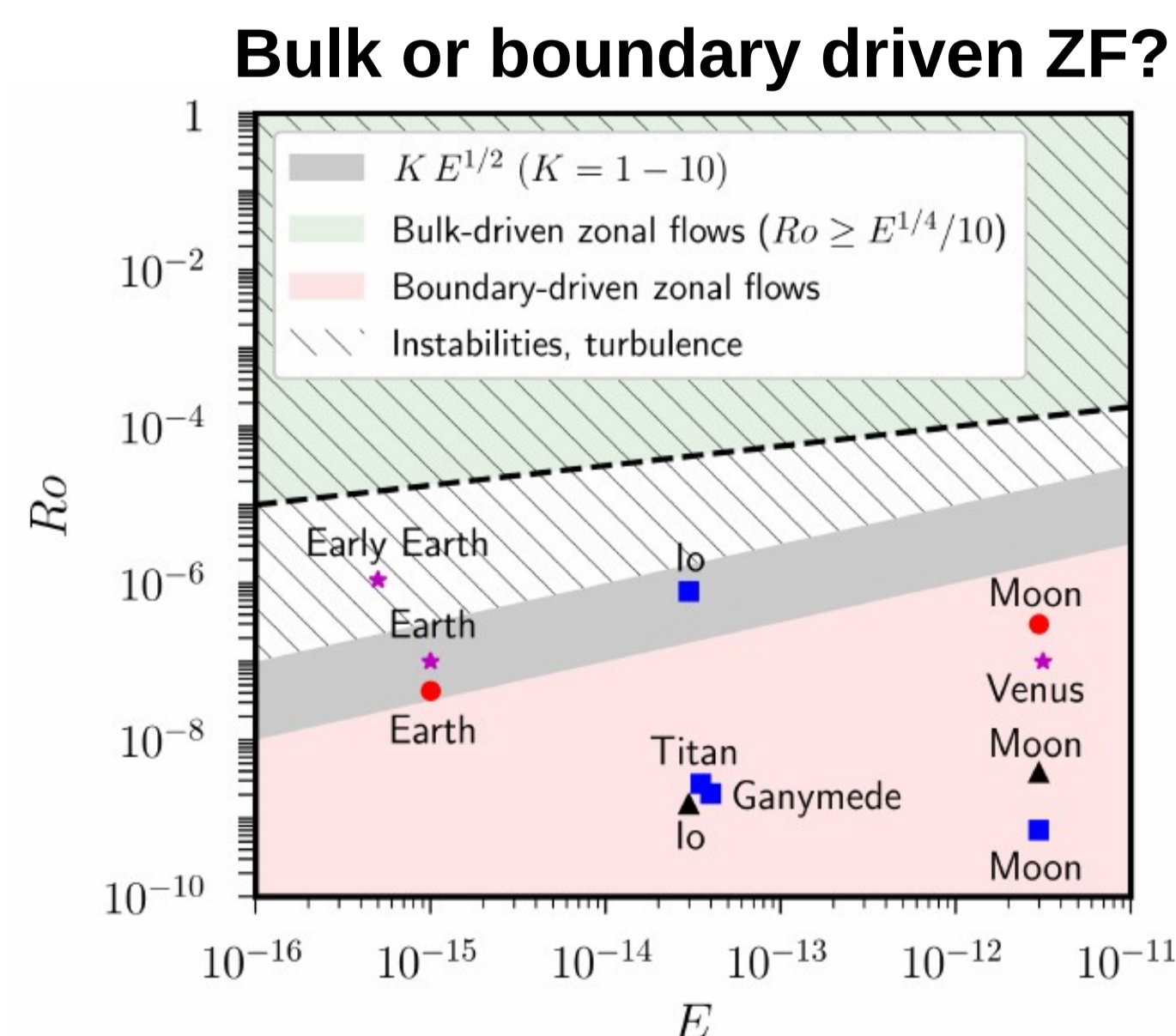
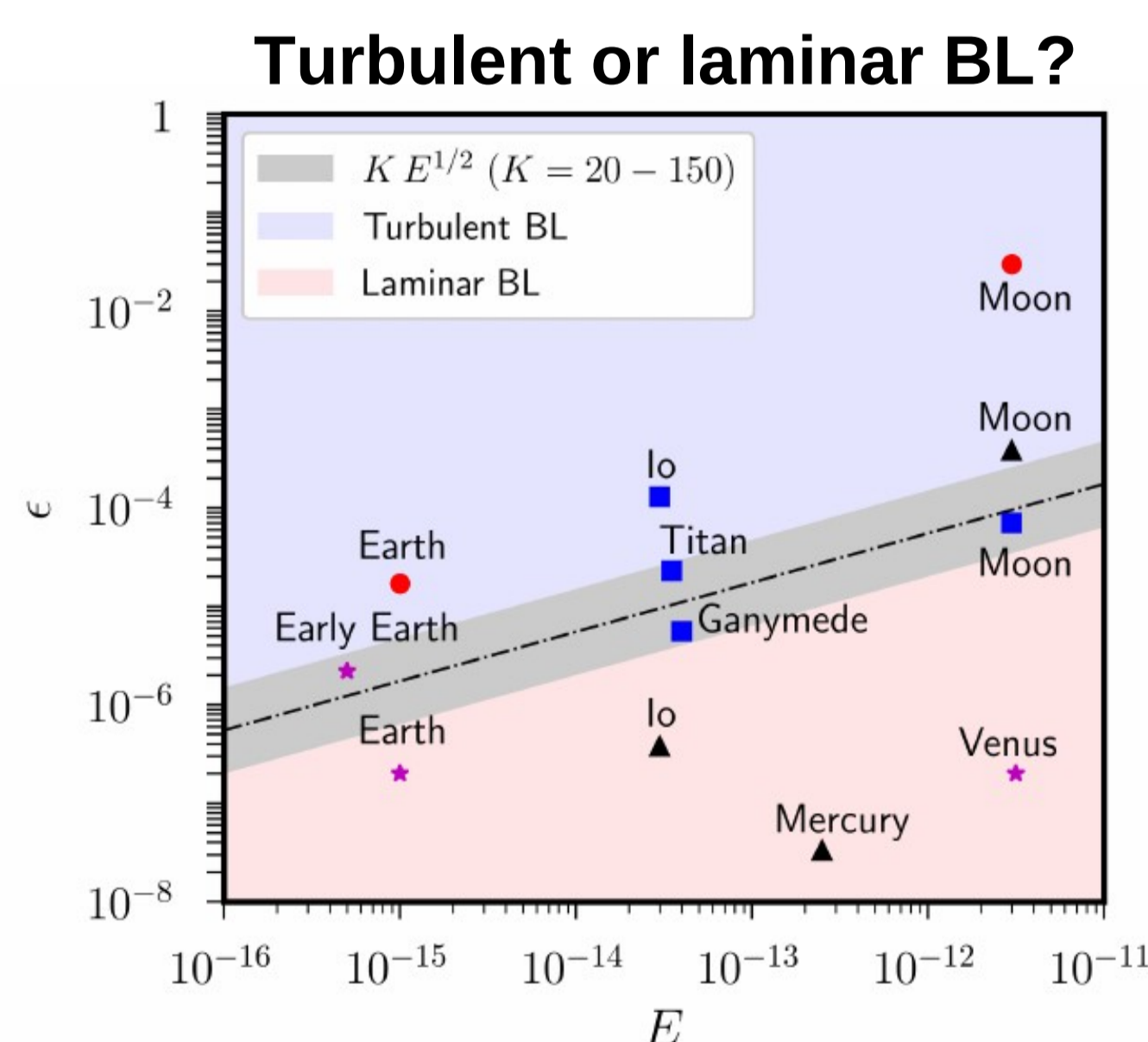
Geostrophic shear (GS) at critical latitudes



- **$E^{-1/2}$ scaling** when the GS enters the Ekman layer (at $s \sim 1$, for $\omega \sim 0$)
- **Previously proposed⁶ $E^{-1/10}$ scaling valid** for various frequencies & forcings

But for precession $\delta u_g / \epsilon^2 \propto E^{-3/10}$... **Why?**

ZF in planets & moons



Red circles: precession. Blue squares: longitudinal librations. Black triangles: latitudinal librations. Magenta stars: tides. – Rossby number $Ro = \mathcal{O}(\beta)$ for tides or $Ro = \mathcal{O}(\beta)$ for precession & libration, with β the typical boundary (equatorial or polar) ellipticity.

- Both **laminar & turbulent** boundary layers (BL) can be expected
- **Bulk-driven ZF** are likely **irrelevant**

=> **Our theoretical ZF (based on laminar BL) is expected in several bodies**

REFERENCES

1. Roberts & Aurnou, 2012. Geophys. Astrophys. Fluid Dyn. 106 (2), 157–230.
 2. Sauret et al., P. 2014. Geophys. Res. Lett. 41 (17), 6078–6083.
 3. Favier et al, 2014. Mon. Not. R. Astron. Soc. 439 (1), 845–860.
 4. Cébron et al., 2021. J. Fluid Mech., 916, A39, 2021.

Zonal flows due to fingering convection⁵

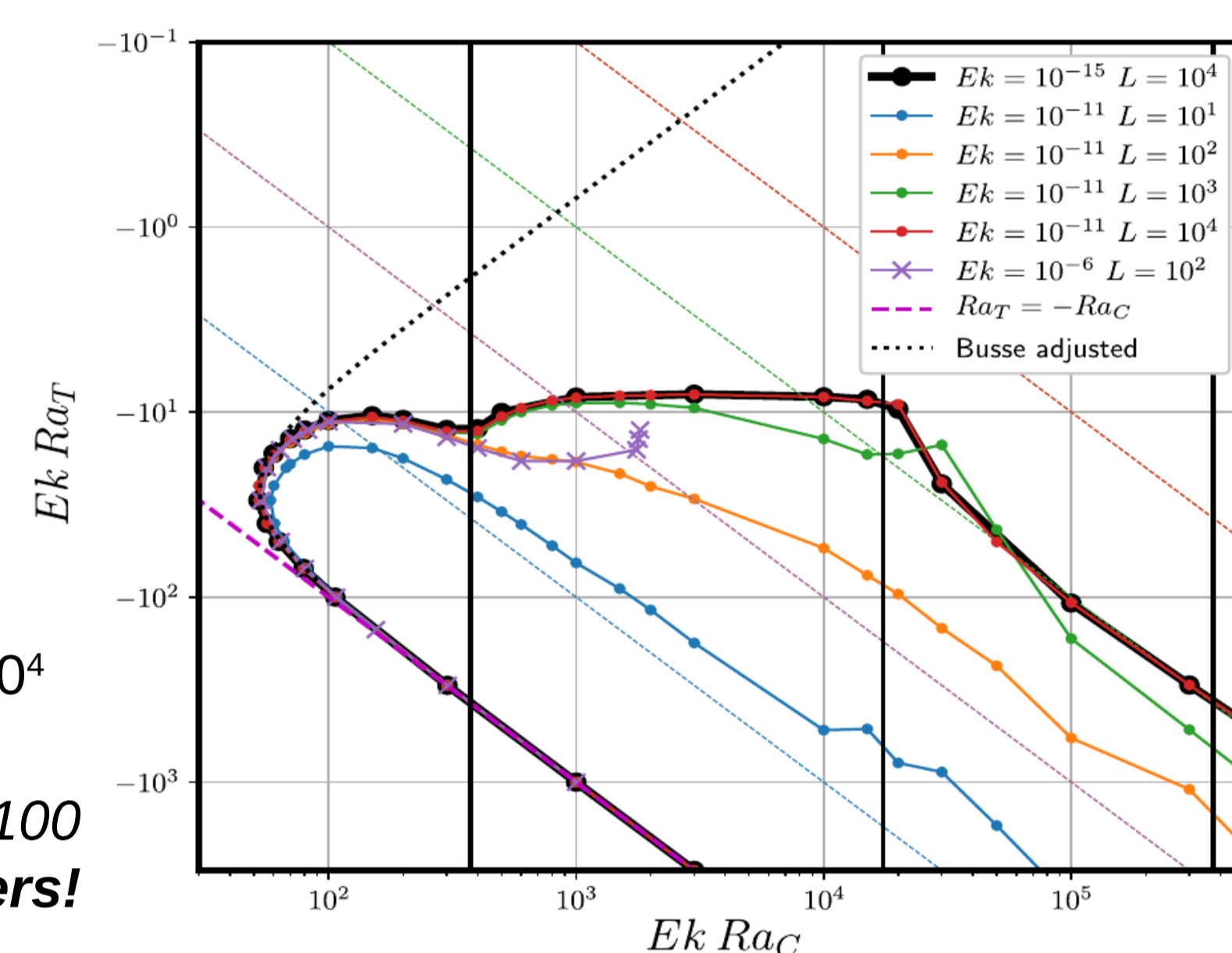
Problem, method & onset

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\frac{2}{Ek} \mathbf{1}_z \times \mathbf{u} - \nabla p + \nabla^2 \mathbf{u} + (Ra_T \Theta + Ra_C \xi) r \mathbf{1}_r,$$

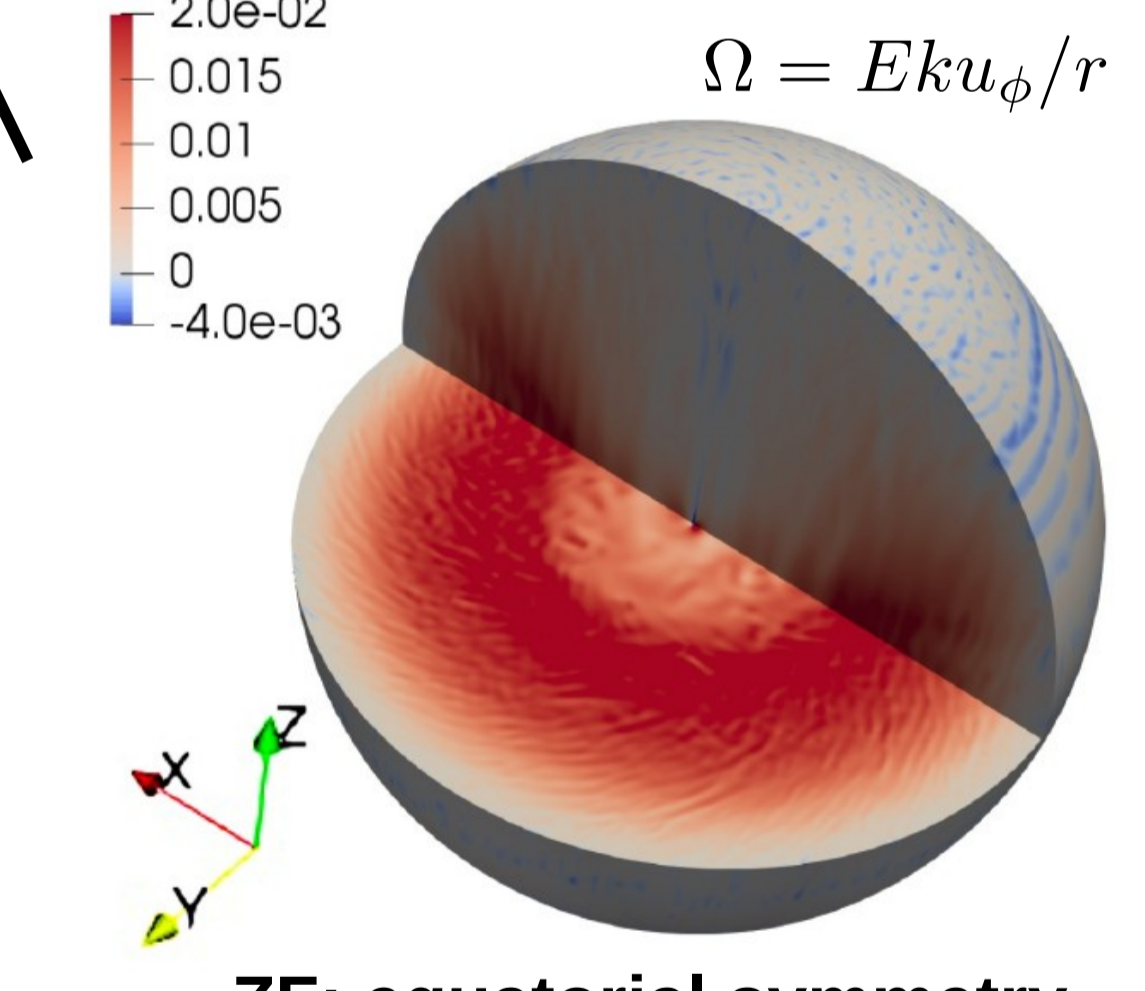
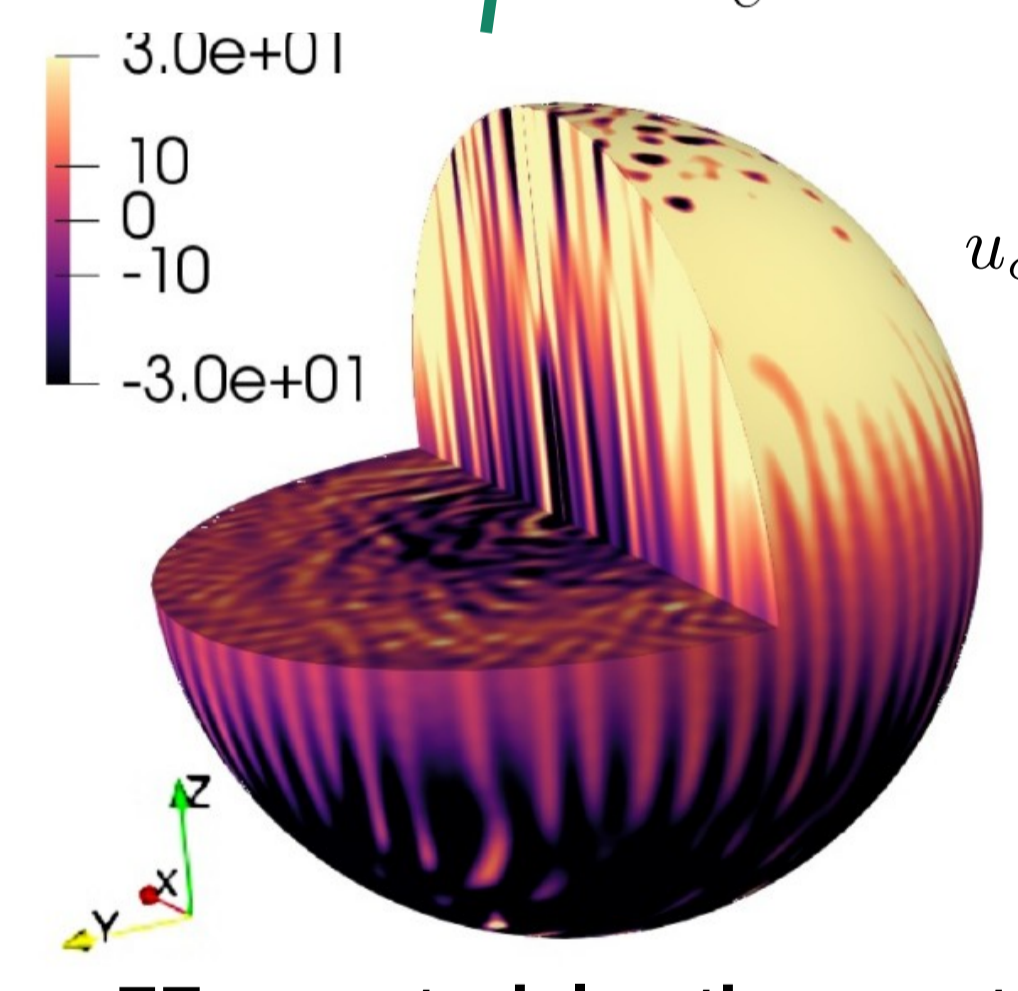
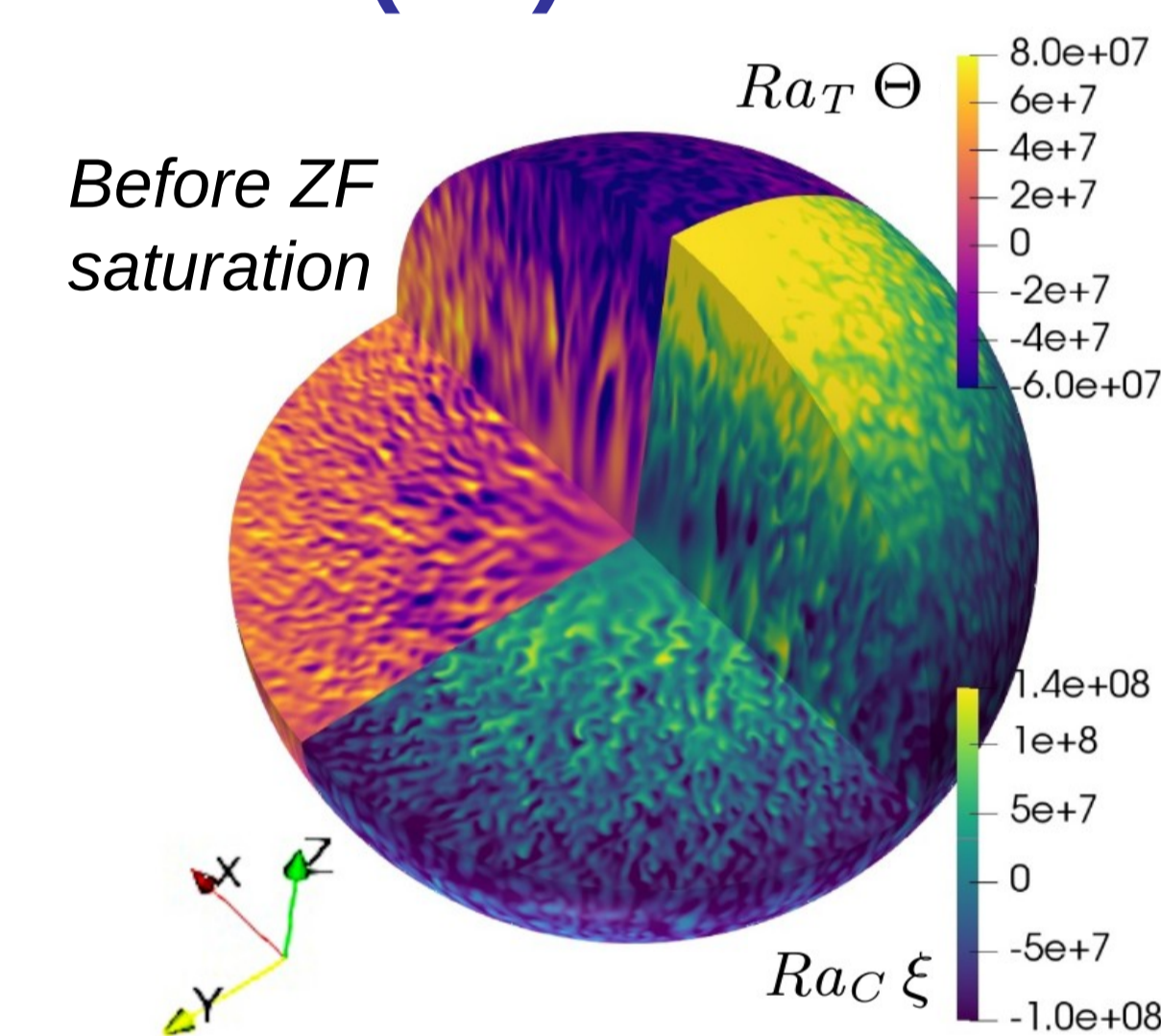
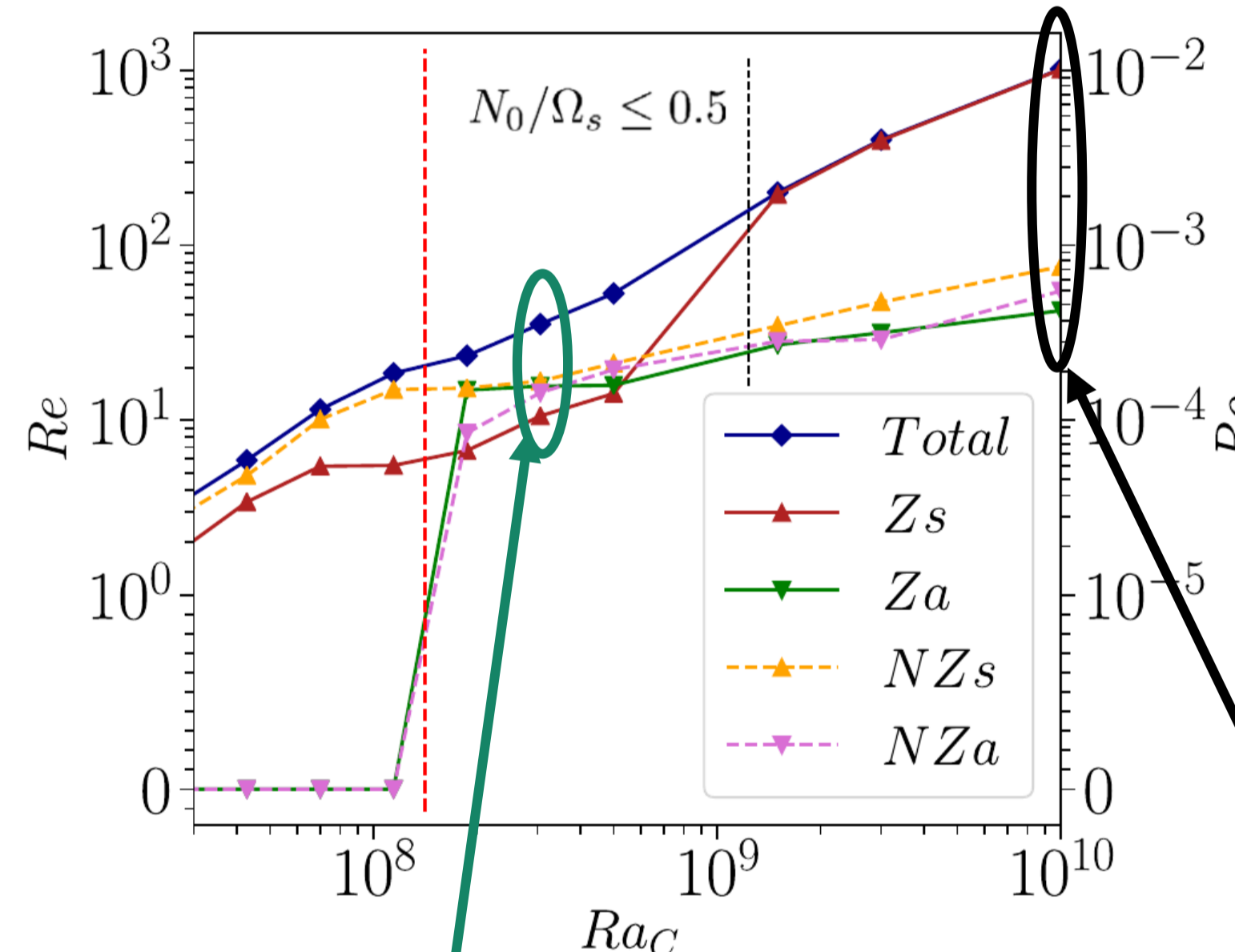
$$\frac{\partial \Theta}{\partial t} + (\mathbf{u} \cdot \nabla) \Theta = \frac{1}{Pr} (2 \mathbf{r} \cdot \mathbf{u} + \nabla^2 \Theta),$$

$$\frac{\partial \xi}{\partial t} + (\mathbf{u} \cdot \nabla) \xi = \frac{1}{Sc} (2 \mathbf{r} \cdot \mathbf{u} + \nabla^2 \xi),$$

- **Full sphere, radial gravity**
 - **Internal sources of buoyancy**
 - **Boundary: no-slip & fixed flux**
 - **SINGE⁷**: linear eigensolver (onset)
 - **XSHELLS⁸**: time step nonlinear eq.
 - **Earth**: $Ek=10^{-15}$, $Sc=10^2-10^3$, $L=Sc/Pr=10^4$
- $m=1$ (onset), $Sc=100$
 => **Reach Earth's core parameters!**



Fingering & zonal flows (ZF)



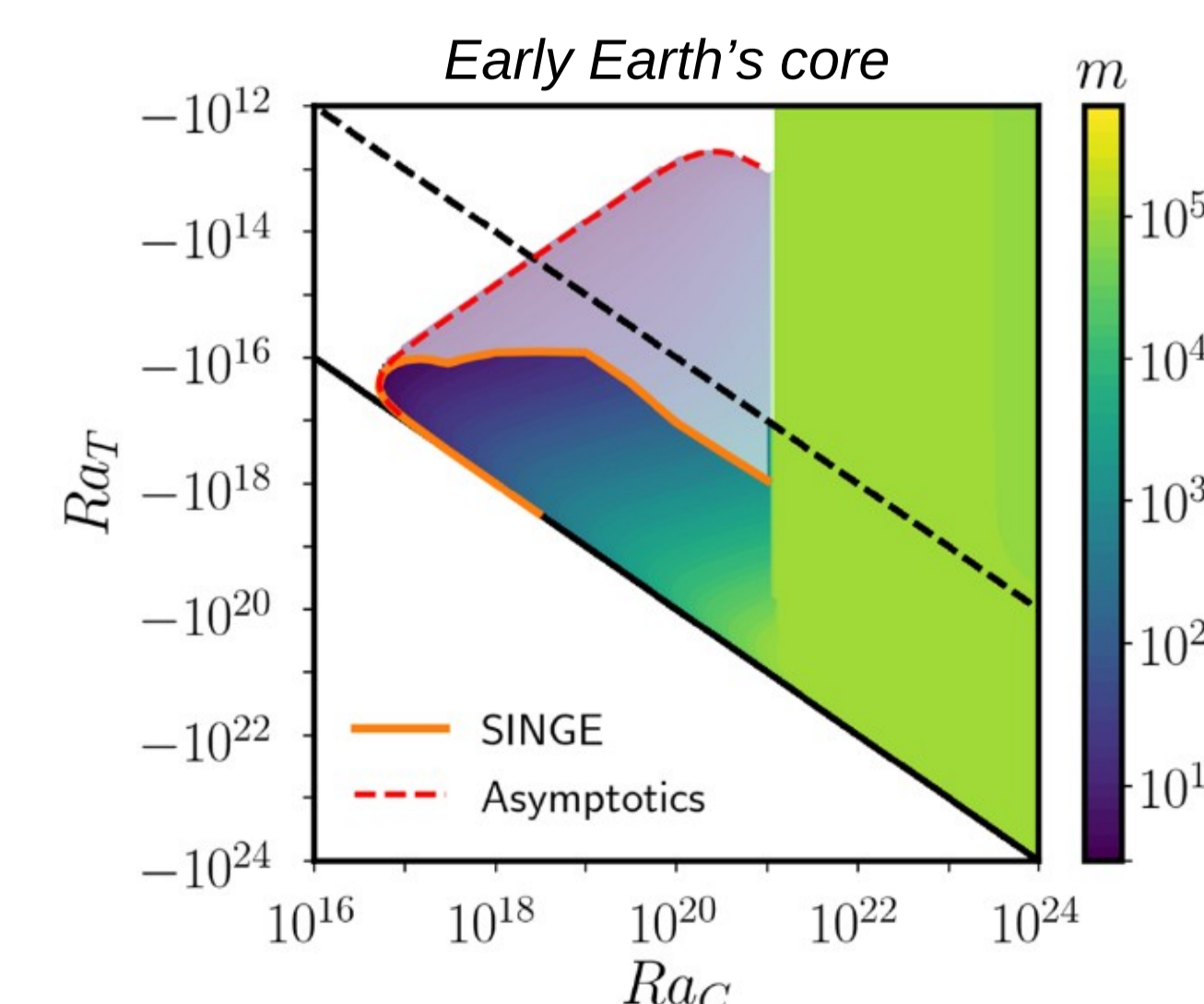
ZF: equatorial antisymmetry

ZF: equatorial symmetry

Fingering & ZF in the Early Earth's core ?

- **Double-diffusion** is only key for $Ra_r \sim -Ra_c$
- **Early Earth's core onset** reduced from $Ra_c \sim 10^{21}$ to 10^{17} (by the thermal field)
- Suggest that the **early Earth core** was prone to **turbulent RDDC**, with **large-scale ZF**
- Confirmed in spherical shells by C. Guervilly (<https://arxiv.org/abs/2205.01761>): ZF exceed the non-axisymmetric flow for large Ra

=> **Perspective: magnetic field effect?**



5. Monville et al., 2019. Geophys. J. Int. 219, S195–S218.
 6. Lin & Noir, 2021. Geophys. Astrophys. Fluid Dyn. 115 (3), 258–279.
 7. <https://bitbucket.org/vidalje/singe>
 8. <https://nschaeff.bitbucket.io/xshells/>