

Topographic drag at the core-mantle interface

¹Rémy Monville, ²David Cébron, ²Dominique Jault

¹University of California, Los Angeles, ²Université Grenoble Alpes, CNRS, ISTerre

Description of the problem

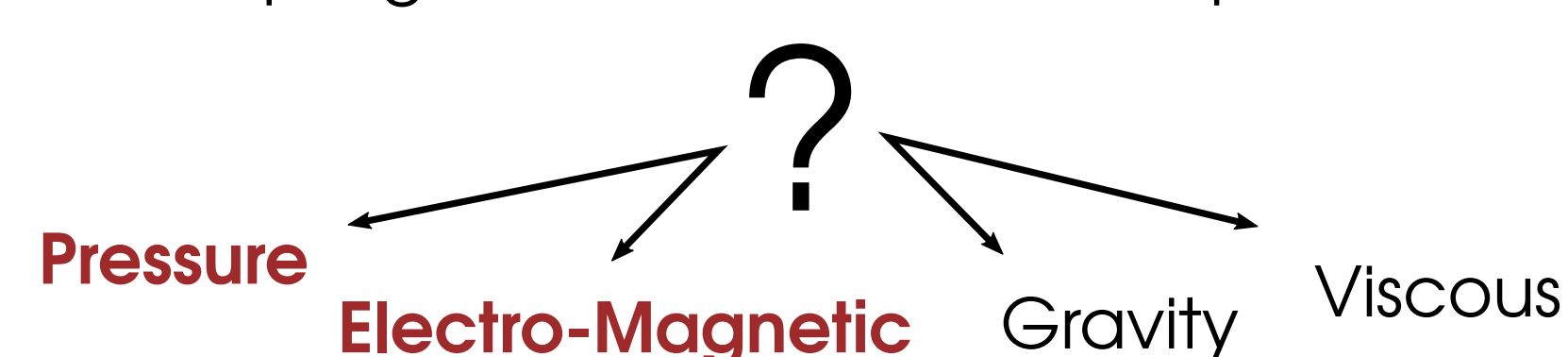
Earth and Moon's rotations are tracked accurately, and data are inverted with rotation models

This provide **coupling** values between the outer core and the mantle/the inner core

Forward physical models failed to explain:

- decadal changes in the **Length-of-Day** and the concomitant changes in axial core angular momentum
- out of phase component of the **retrograde annual nutation**

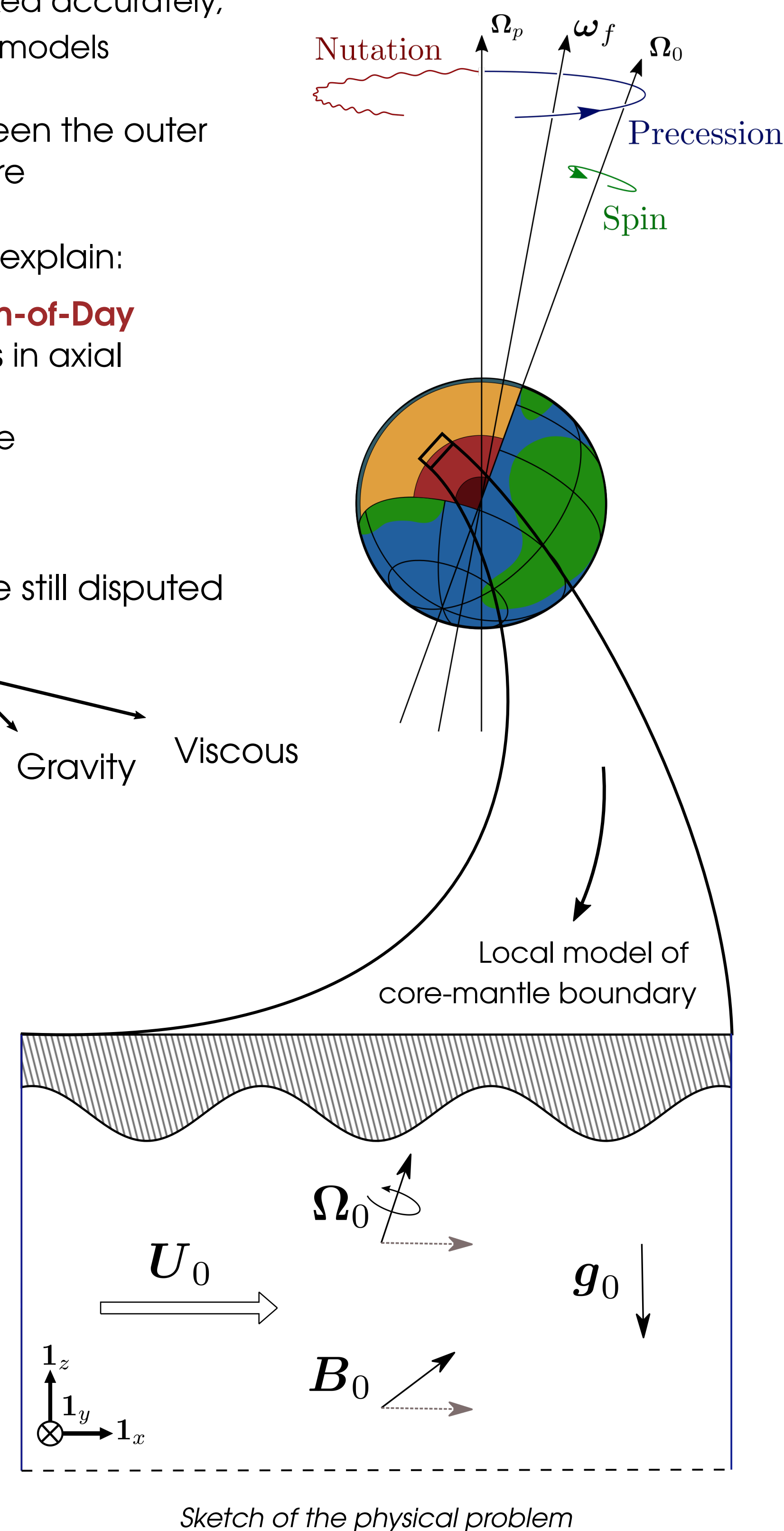
Coupling mechanisms are still disputed



Key effects:

- Stratification
- Magnetic field
- Rotation

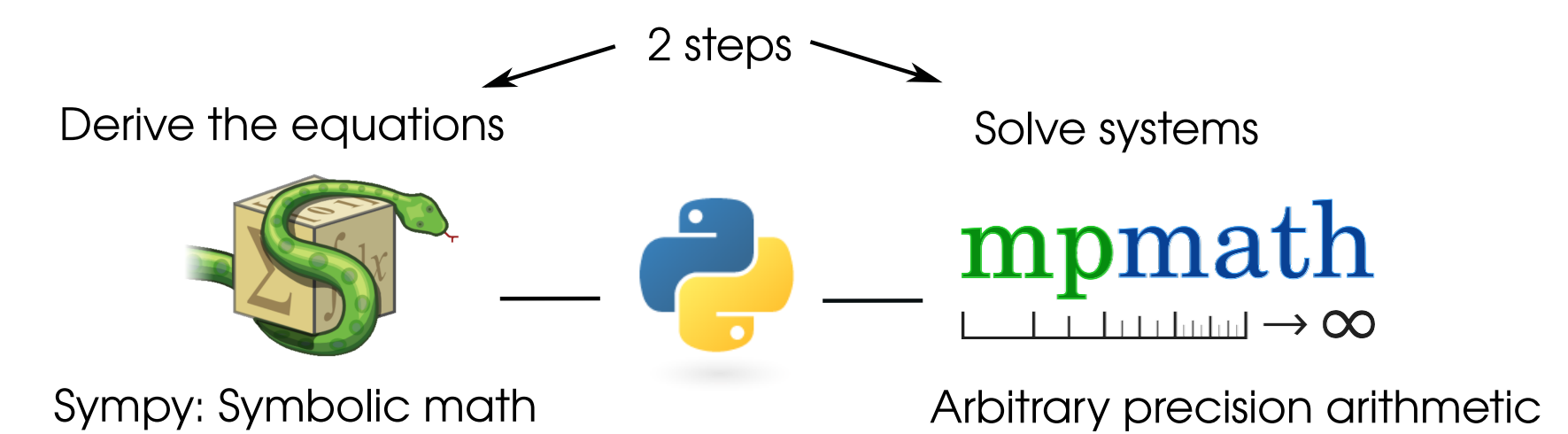
Modelling the topographic **core-mantle coupling** is a long-standing issue dating back to Hide (1969)¹ or Braginsky (1998)². By first following the recent work of Glane & Buffett (2018)³ and Jault (2020)⁴ on the LOD, we revisit the **Cartesian perturbative models** of **incompressible Boussinesq** hydro-magnetic flow over a **bumpy topography**.



Sketch of the physical problem

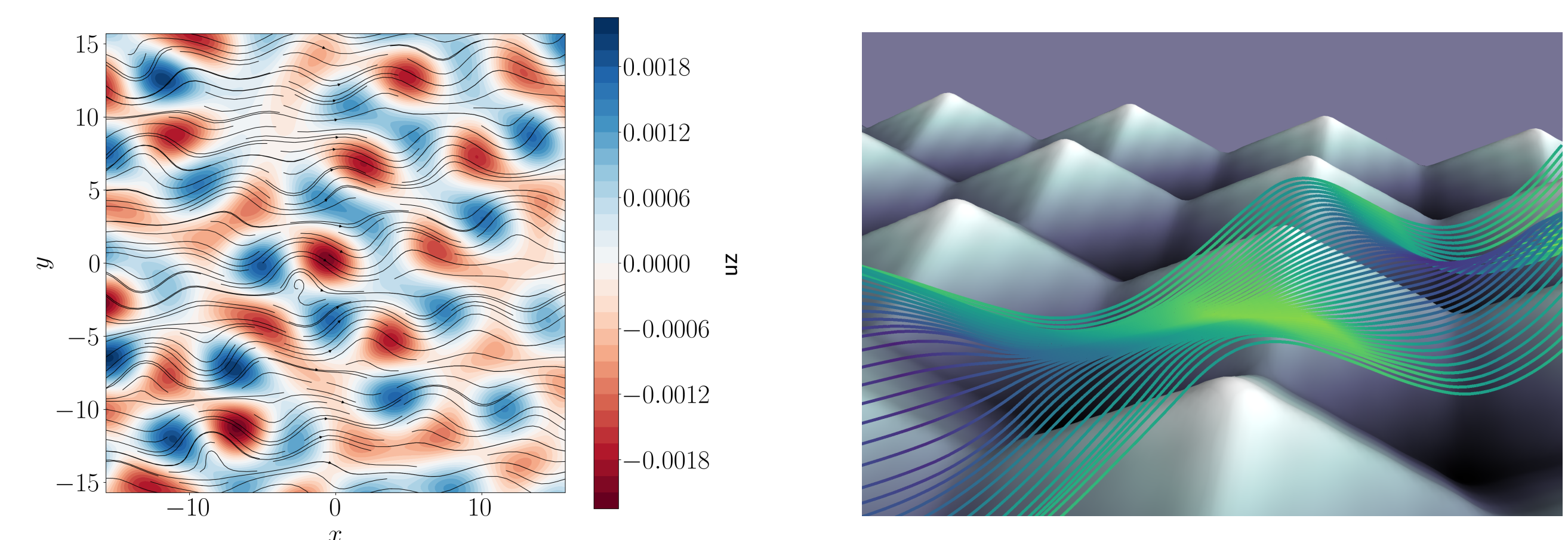
Methods

Our code **ToCCo** rely on symbolic and arbitrary precision calculations

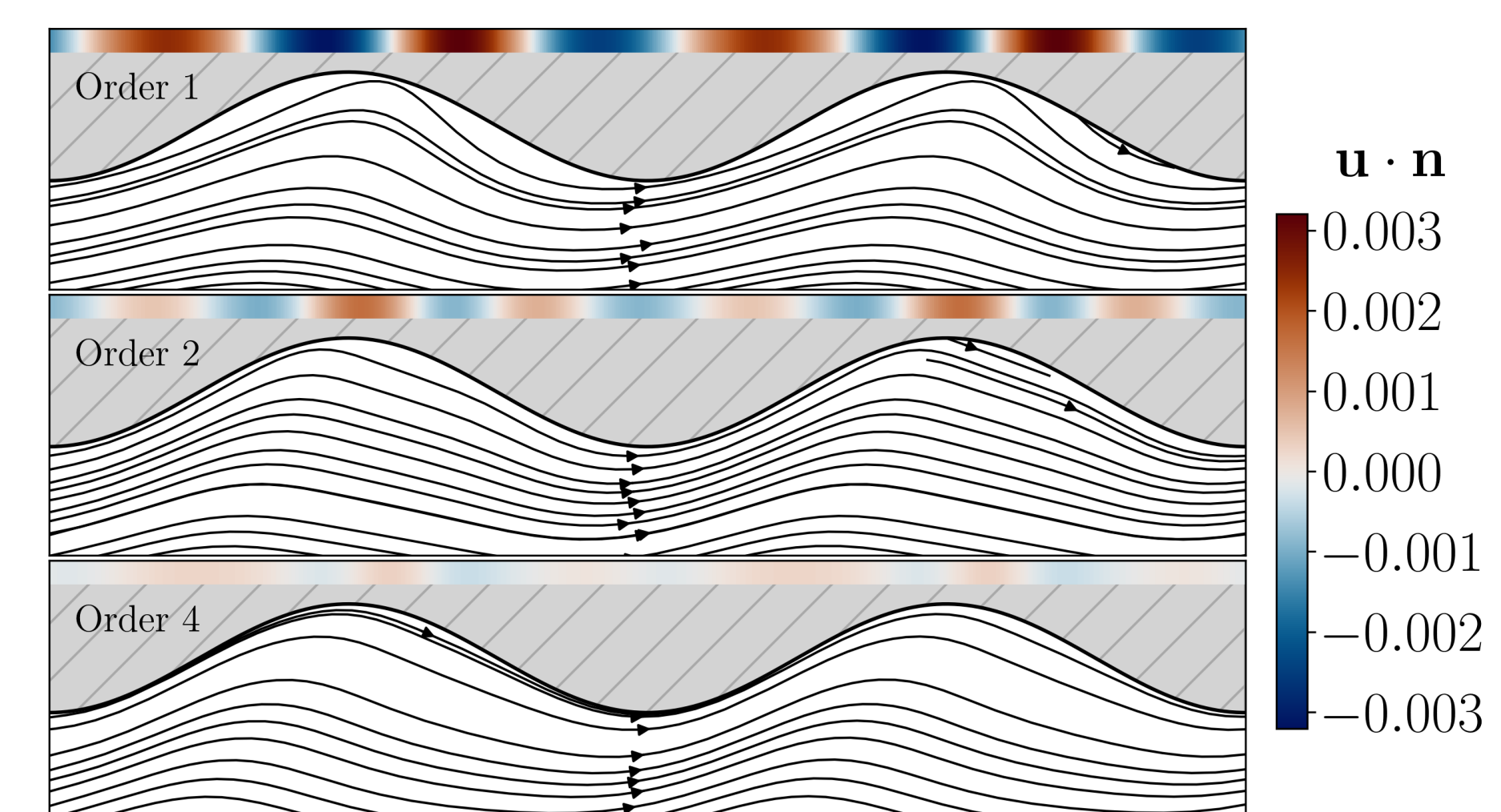


Equations are derived with a **perturbative** approach and **plane waves** approximation

We can explore **arbitrary topography** decomposed into Fourier series



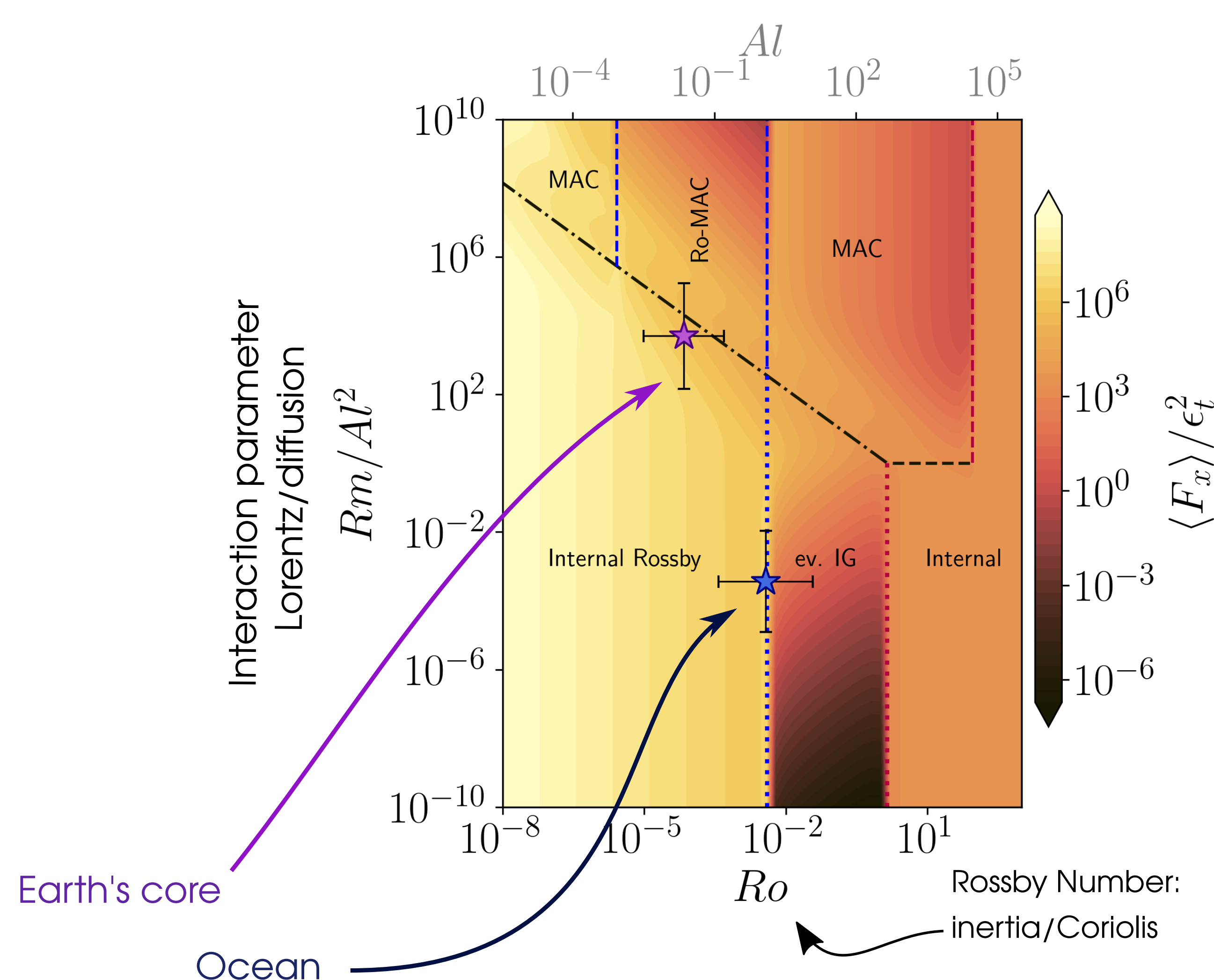
Our **"higher-order"** solutions go beyond the **forced wave** linear regime by investigating **non-linear effects**.



Results

Topographic wave drag

Stress variations with physical parameters of the problem are non-trivial, and it turns out, that the Earth's core is unexpectedly at the frontiers of various regimes.



These variations are due to transitions between stress dominated by **ohmic dissipation** or by the **wave drag** due to the propagation of the **various hydromagnetic waves**.

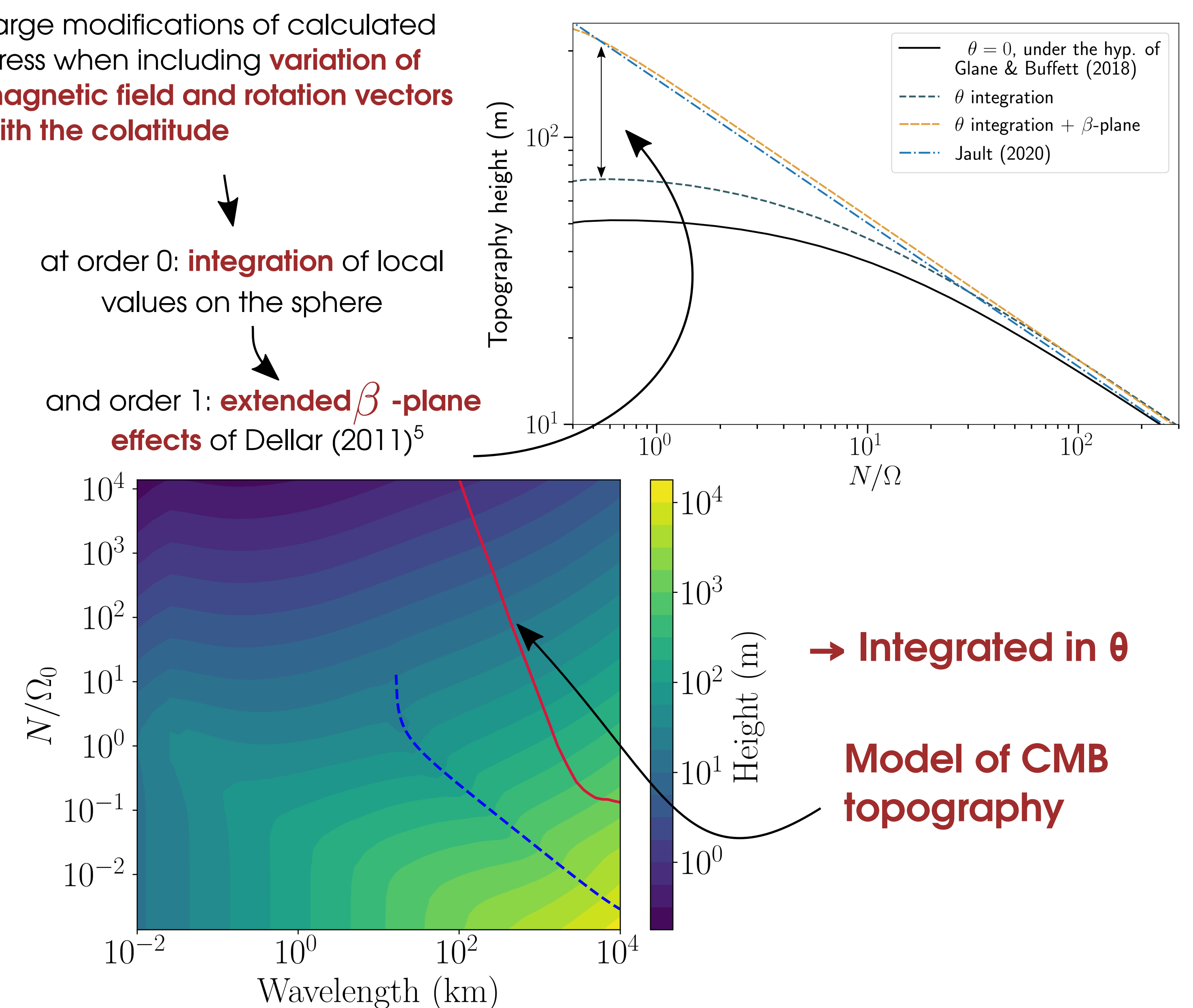
Data : application to length of the day

Parameters needed to obtain **the nominal value** for mean longitudinal stress⁴ : 0.027 N.m⁻²

Large modifications of calculated stress when including **variation of magnetic field and rotation vectors with the colatitude**

at order 0: **integration** of local values on the sphere

and order 1: **extended β -plane effects** of Dellar (2011)⁵



→ Integrated in θ
Model of CMB topography



@monville

remy.monville@epss.ucla.edu

ToCCo:



[1] R. Hide, *Nature* 1969, 222, 1055.

[2] S. I. Braginsky, *Earth, Planets and Space* 1998, 50, 641.

[3] S. Glane, B. Buffett, *Frontiers in Earth Science* 2018, 6.

[4] D. Jault, *Geophysical Journal International* 2020, 221, 951

[5] P. J. Dellar, *Journal of Fluid Mechanics* 2011, 674, 174.

Our paper : R.Monville et al., *JGR Solid Earth* 2025 (published soon)